

# On Section 3 of "What explains the 2007-09 drop in employment?"

by Atif Mian and Amir Sufi, *Econometrica*, Nov. 2014.

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## From Mian and Sufi's abstract

- Deterioration in household balance sheets, or the *housing net worth channel*, played a significant role in the sharp decline in U.S. employment 2007-09.
- Counties with a larger decline in housing net worth experienced a larger decline in non-tradable employment.
- Result not driven by industry-specific supply side shocks, policy-induced business uncertainty, or credit supply tightening.
- No significant expansion of the tradable sector in counties with the largest decline in housing net worth.
- Little evidence of wage adjustment within or emigration out of the hardest hit counties.

# A simple partial-equilibrium model

$m$  counties,  $i = 1, 2, \dots, m$ ; may differ w.r.t. housing net worth.

Same size = 1 = labor supply in each county.

*In each county two sectors:*

Sector  $N$  produces a *non-tradable good* (only sold at the local market).

-  $T$  - *tradable good* (sold economy-wide at one price).

Labor homogeneous, immobile across counties, mobile across sectors within a county.

Production capital not considered.

Houses are treated as non-produced land. Focus is on the channel from a fall in housing net worth to non-tradables production independently of an effect on construction.

*Preferences:*  $U(c^N, c^T) = \alpha \log c^N + (1 - \alpha) \log c^T$ . Hence,

$$P_i^N c_i^N = \alpha D_i,$$

$$P^T c_i^T = (1 - \alpha) D_i,$$

where  $D_i =$  nominal consumption demand at  $i$ .      *Production:*

$$y_i^N = a e_i^N,$$

$$y_i^T = b e_i^T.$$

*Walrasian general equilibrium:* Households and firms are price takers, markets clear by price adjustment:

$W_i = P_i^N a = P^T b \equiv W$ ,    hence     $P_i^N = P^N \quad \forall i$ , and  $P^N / P^T = b/a$ .

$$e_i^N + e_i^T = 1, \quad \forall i,$$

$$y_i^N = c_i^N = \alpha D_i / P_i^N = \alpha D_i / P^N, \quad \forall i,$$

$$y_i^T \neq c_i^T \text{ generally, since } D_i\text{'s may differ,}$$

$$\text{but } \sum_{i=1}^m y_i^T = \sum_{i=1}^m c_i^T = \frac{(1 - \alpha) \sum_{i=1}^m D_i}{P^T}.$$

Money neutrality!

## Determination of $P^T$ , $P^N$ , and sectoral allocation of employment

$$\begin{aligned}\sum_{i=1}^m y_i^T &= \sum_{i=1}^m b e_i^T = b \sum_{i=1}^m (1 - e_i^N) = b \sum_{i=1}^m \left(1 - \frac{y_i^N}{a}\right) = b \sum_{i=1}^m \left(1 - \frac{\alpha D_i}{a P^N}\right) \\ &= b \left(m - \frac{\alpha \sum_{i=1}^m D_i}{a P^N}\right) = \frac{(1 - \alpha) \sum_{i=1}^m D_i}{P^T}.\end{aligned}$$

So

$$P^T = \frac{\sum_{i=1}^m D_i}{b m}, \quad P^N = \frac{\sum_{i=1}^m D_i}{a m}, \quad W = P^T b = P^N a. \quad (*)$$

$$e_i^N = \frac{y_i^N}{a} = \frac{\alpha D_i}{a P^N}, \quad e_i^T = 1 - \frac{\alpha D_i}{a P^N}, \quad \forall i. \quad (**)$$

Assume initial symmetry,

$$\begin{aligned}D_i &= D_0, \quad i = 1, 2, \dots, m. && \text{Then,} \\ P^{*T} &= \frac{D_0}{b}, \quad P^{*N} = \frac{D_0}{a}, \quad W^* = P^{*T} b = D_0, \\ e_i^{*N} &= \frac{\alpha D_0}{a P^{*N}} = \alpha, \quad e_i^{*T} = 1 - \alpha, \quad \forall i.\end{aligned}$$

**Negative demand shock.** Suppose, a negative shock to housing net worth occurs, perhaps due to a bursting housing bubble. Suppose further that this triggers a tightening of borrowing constraints on indebted households.

As a result, to a varying degree across counties, households' nominal demand falls.

Let initial uniform demand,  $D_0$ , equal 1, so that

$$D_i = 1 - \delta_i, \quad \forall i \quad \delta_i \in (0, 1).$$

Average shock is

$$\frac{\sum_{i=1}^m \delta_i}{m} \equiv \bar{\delta}.$$

Non-tradable employment relies heavily on local demand, while tradable employment relies on national or even global demand.

## Case 1: Complete nominal price flexibility.

$$\sum_{i=1}^m D_i = \sum_{i=1}^m (1 - \delta_i) = m - \sum_{i=1}^m \delta_i = m - m\bar{\delta} = m(1 - \bar{\delta})$$

Prices fall in proportion to fall in nominal demand:

$$P^T = \frac{1 - \bar{\delta}}{b} \quad \text{and} \quad P^N = \frac{1 - \bar{\delta}}{a},$$
$$W = aP^N = bP^T = 1 - \bar{\delta}.$$

Still  $e_i^N + e_i^T = 1$  (full employment  $\forall i$ ), but with local sectoral reallocation:

$$e_i^T = 1 - \frac{\alpha(1 - \delta_i)}{1 - \bar{\delta}} \begin{cases} \geq e_i^{*T} (= 1 - \alpha) & \text{for } \delta_i \geq \bar{\delta}, \\ \leq e_i^{*T} (= 1 - \alpha) & \text{for } \delta_i < \bar{\delta}, \end{cases} \text{ respectively,}$$

$$e_i^N = \frac{y_i^N}{a} = \frac{\alpha D_i}{aP^N} = \frac{\alpha(1 - \delta_i)}{1 - \bar{\delta}} \begin{cases} \leq e_i^{*N} (= \alpha) & \text{for } \delta_i \geq \bar{\delta}, \\ \geq e_i^{*N} (= \alpha) & \text{for } \delta_i < \bar{\delta}, \end{cases} \text{ respectively.}$$

*Predictions:* Still full employment everywhere. In counties faced by a large local shock workers move from N-employment to T-employment. The reverse if shock is small.

## Case 2: Complete nominal price rigidity

$$P^T = \frac{D_0}{b} = \frac{1}{b}, \quad P^N = \frac{D_0}{a} = \frac{1}{a}.$$

From (\*\*):

Tradables:

$$\sum_{i=1}^m y_i^T = \frac{(1-\alpha) \sum_{i=1}^m D_i}{P^T} = \frac{(1-\alpha)m\bar{D}_i}{P^T} = \frac{(1-\alpha)m(1-\bar{\delta})}{P^T}$$

$$e_i^T = \frac{y_i^T}{b} = \frac{\sum_{i=1}^m y_i^T}{mb} = \frac{(1-\alpha)(1-\bar{\delta})}{P^T b} = (1-\alpha)(1-\bar{\delta})$$
$$< e_i^{*T} = 1 - \alpha, \quad \forall i.$$

hence T-fall  $\equiv e_i^{*T} - e_i^T = 1 - \alpha - (1-\alpha)(1-\bar{\delta}) = (1-\alpha)\bar{\delta}$ .

Non-tradables:

$$e_i^N = \frac{\alpha D_i}{a P^N} = \frac{\alpha(1-\delta_i)}{1} < e_i^{*N} = \alpha, \quad \forall i,$$

hence N-fall  $\equiv e_i^{*N} - e_i^N = \alpha - \alpha(1-\delta_i) = \alpha\delta_i$ .

## Predictions:

1. Fall in total employment.
2. Fall in local T-employment should have no corr. with local shock  $\delta_i$ .
3. Fall in local N-employment should have pos. corr. with local shock  $\delta_i$ .

Data complies.

Likely explanation:

Lower housing net worth  $\Rightarrow$  lower wealth

$\Rightarrow \left\{ \begin{array}{l} \text{consumption } \downarrow \\ \text{value of collateral } \downarrow \Rightarrow \text{credit contraction} \end{array} \right\} \Rightarrow \text{consumption } \downarrow\downarrow$

$\Rightarrow \text{investment } \downarrow \Rightarrow \text{consumption } \downarrow\downarrow\downarrow$

and so on in a vicious circle.

## NOTES

Sizes of the adverse demand shocks are ordered in this way:

$$\delta_i < \delta_{i+1}, \quad i = 1, 2, \dots, m - 1,$$

but of no use here.

Case 2:

*Total* employment in county  $i$  is

$$e_i = e_i^T + e_i^N = (1 - \alpha)(1 - \bar{\delta}) + \alpha(1 - \delta_i) < 1 = e_i^*.$$

Fall in total employment in county  $i$  is

$$1 - e_i = 1 - ((1 - \alpha)(1 - \bar{\delta}) + \alpha(1 - \delta_i)) = (1 - \alpha)\bar{\delta} + \alpha\delta_i.$$

*Prediction:*

Fall in total local employment should have pos. corr. with local shock  $\delta_i$ .

Data complies (no surprise given the above).