

Economics of Banking

Lecture 16

April 2023

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A simple model of risky banking

Investment projects may have a liquidation value:

Two banks in two periods $t = 0, 1, 2$.

Investment: R in next period with probability π , 0 otherwise.

Payoffs independent over time, but industry-dependent.

Banks have specific skills: When the investment is done by a non-bank, it yields $R - \Delta$.

Banks have fully insured deposits.

Bank failures

Expected net outlays of the insurer:

(1) FF (two failures): Banks sold to private investors, paying at most

$$\underline{p} = \pi(R - \Delta - 1)$$

(2) SF or FS (one fails and the other succeeds):, The other bank which take over the assets and can get

$$\bar{p} = \pi(R - 1)$$

but may pay less, namely p^* with

$$\underline{p} < p^* < \bar{p}.$$

(3) SS (both banks succeed): no liquidation.

Insurance premium

The premium depends on the correlation between banks

If they invest in the same industry, then probability of FF at $t = 1$ is π .

Expected net outlays net outlays of the insurance:

$$q_s = (1 - \pi)(1 - \underline{p}),$$

If they invest in different industries, then expected net outlays are instead

$$q_d = \pi(1 - \pi)(1 - p^*) + (1 - \pi)^2(1 - \underline{p}) = q_s - \pi(1 - \pi)(p^* - \underline{p}).$$

Fair premium depends on correlation!

Other factors influencing premium

Suppose that bank 1 is small and bank 2 is large:

If 1 fails, 2 may take over at some price p° with $\underline{p} < p^\circ < \bar{p}$, and the expected net outlays of the insurance is

$$q^\circ = \pi(1 - \pi)(1 - p^\circ) + (1 - \pi)^2(1 - \underline{p}) < (1 - \pi)(1 - \underline{p}),$$

If 2 fails, 1 is too small to take over its investments, and the fair premium for 2 is $(1 - \pi)(1 - \underline{p})$.

Thus, the fair premium is smaller for 1 than for 2.

Possibility of bailout

Suppose that there is a lender of last resort (next chapter), supplying credits to banks at social cost c .

Bailing out if FF gives $\pi R - 1 - c$ per bank, liquidating gives a loss of $\pi\Delta$.

Premium if banks choose the same industry are

$$\bar{q}_s = (1 - \pi) [(1 - \underline{p}) + \min\{\pi\Delta, c\}]$$

and if different industries

$$\bar{q}_d = \pi(1 - \pi)(1 - p^*) + (1 - \pi)^2 [(1 - \underline{p}) + \min\{\pi\Delta, c\}].$$

We have $\bar{q}_s > q_s$, $\bar{q}_d > q_d$, and $\bar{q}_s > \bar{q}_d$. Finally:

$$\bar{q}_s - \bar{q}_d > q_s - q_d,$$

Difference becomes greater when all costs are taken into consideration.

Incentive compatibility

Premiums \hat{q}_s and \hat{q}_d designed so that banks to choose uncorrelated investments:

Profits if the banks invest in the same industry:

$$\Pi_s = \pi E \left[\tilde{\Pi}_2 | SS \right] + (1 - \pi) E \left[\tilde{\Pi}_2 | FF \right] - \hat{q}_s,$$

and if they invest in different industries

$$\Pi_d = \pi E \left[\tilde{\Pi}_2 | SS \right] + \pi(1 - \pi) E \left[\tilde{\Pi}_2 | SF \right] + (1 - \pi)^2 E \left[\tilde{\Pi}_2 | FF \right] - \hat{q}_d.$$

We have

$$E \left[\tilde{\Pi}_2 | SF \right] = E \left[\tilde{\Pi}_2 | SS \right] + (\bar{p} - p^*),$$

so that

$$\Pi_d = \pi E \left[\tilde{\Pi}_2 | SS \right] + \pi(1 - \pi)(\bar{p} - p^*) + (1 - \pi)^2 E \left[\tilde{\Pi}_2 | FF \right] - \hat{q}_d.$$

Incentive compatibility II

Then

$$\Pi_s - \Pi_d = \pi(1 - \pi) \left[E \left[\tilde{\Pi}_2 | FF \right] - (\bar{p} - p^*) \right] + \hat{q}_d - \hat{q}_s.$$

and we can solve to get

$$\hat{q}_s = \pi(1 - \pi) \left[E \left[\tilde{\Pi}_2 | FF \right] - (\bar{p} - p^*) \right] + \hat{q}_d.$$

Surcharge for correlated investments depends on the subsidy received through a bailout, which is

$$E \left[\tilde{\Pi}_2 | FF \right]$$

and on discount given to the surviving bank if only one failure.

Another model of banking

There are N households and μ banks, each endowed with 1 unit of money.

Investment gives a payoff $R > 0$ with probability p_L , 0 otherwise.

Households may invest on their own or sign a (deposit) contract with a bank taking care of investment.

Banks can choose to be *sound*: Success probability is $p_H = p_L + \Delta p > p_L$ at a cost C ,

The households cannot observe whether a bank is sound or unsound.

Banks are allowed to invest their own unit and $k - 1$ units of deposit money.

Incentive compatibility

Banks get a fee Q from the depositors.

Banks taking deposits k will be sound only if

$$[R + Q(k - 1)]p_H - Ck \geq [R + Q(k - 1)]p_L,$$

or equivalently

$$Q \geq \frac{Ck - R\Delta p}{(k - 1)\Delta p}$$

Household demand for deposits

If households believe that the fraction of sound banks is g , then deposits used only if

$$Q \leq \frac{Rg\Delta p}{p_L + g\Delta p} = R - \frac{Rp_L}{p_L + g\Delta p}. \quad (1)$$

We get a region of feasible (k, Q) -pairs:

Introducing deposit insurance

Deposit insurance collects taxes from banks, depositors and individual investors, tax rates are τ_j , for $j = B, D, S$.

Tax revenue is

$$T = \mu\tau_B + N\rho\tau_D + N(1 - \rho)\tau_S.$$

with ρ fraction of households being depositors.

Each bank has $1 - \tau_B$ and can initiate investments to the amount of $k(1 - \tau_B)$, $(k - 1)\mu(1 - \tau_B)$ comes from depositors and from T , assume $T < (k - 1)\mu(1 - \tau_B)$.

After-tax wealth of depositors is $N(1 - \tau_D)$ and not all consumers can be depositors, so

$$\rho = \frac{(k - 1)\mu(1 - \tau_B) - T}{N(1 - \tau_D)} = \frac{\mu[k(1 - \tau_B) - 1]}{N(1 - \tau_S)} - \frac{\tau_S}{1 - \tau_S}.$$

Expected returns

Expected return from investing T , $T(R - Q)(p_L + g\Delta p)$, can be transferred to depositors who get

$$\frac{T}{\rho N}(R - Q)(p_L + g\Delta p) \quad (2)$$

if investment failed.

Bank incentives are as before (measured per unit invested), but household condition for bank use is

$$\rho \left[\frac{T}{\rho N} + (1 - \tau_D) \right] (R - Q)(p_L + g\Delta p) + (1 - \rho)(1 - \tau_S)Rp_L \geq Rp_L(1 - \tau_S).$$

New region of feasible contracts

This condition can be rearranged to

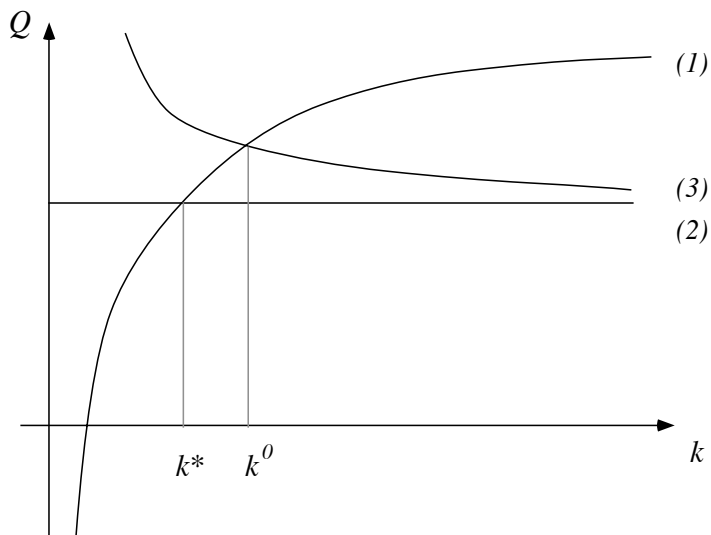
$$Q \leq R - \frac{Rp_L}{p_L + g\Delta p} \frac{\mu(k(1 - \tau_B) - 1) - N\tau_S}{\mu(k(1 - \tau_B) - 1) + \mu\tau_B}.$$

Here

$$\frac{\mu(k(1 - \tau_B) - 1) - N\tau_S}{\mu(k(1 - \tau_B) - 1) + \mu\tau_B} \leq 1$$

increases in k towards 1.

Tax financed deposit insurance increases investment



A case where deposit insurance is suboptimal

As usually, there are three dates, $t = 0, 1, 2$.

Investments:

1. A storage technology,
2. A risky technology, one unit at $t = 0$ yields \tilde{R} at $t = 2$, with

$$\tilde{R} = \begin{cases} \frac{1}{q}R & \text{with probability } q \\ 0 & \text{with probability } 1 - q \end{cases}$$

where q can be chosen by the bank (private information).

Expected payoff is R and variance is

$$\sigma^2(\tilde{R}) = q \left(R - \frac{1}{q}R \right)^2 + (1 - q)R^2 = \frac{1 - q}{q}R^2,$$

decreasing in q , 0 when $q = 1$.

Depositors' choices

Households are impatient with probability π .

If the contracts satisfy standard constraints

$$\begin{aligned} \pi c_1 &= 1 - I, \\ (1 - \pi)c_2 &= I\tilde{R}, \end{aligned} \tag{3}$$

then date 2 expected utility is

$$qu \left(\frac{I}{1 - \pi} \frac{1}{q} R \right) \leq u \left(q \frac{I}{1 - \pi} \frac{1}{q} R \right) = u \left(\frac{I}{1 - \pi} R \right)$$

by concavity of u , so $q = 1$ is optimal.

Socially optimal investment is found by maximizing expected utility subject to (??).

Optimal contracts

Assume that banks maximize the utility of the representative consumer.

The contract will specify withdrawal c_E at date 1 and withdrawal c_L at date 2, outcome risk must be absorbed by the bank.

There is a bank run if depositors observe a signal (a “sunspot”) at $t = 1$, probability of this signal is p .

If the fraction of depositors observing the signal is μ , then we maximize

$$(1 - \mu p) [\pi u(c_E) + (1 - \pi)u(c_L)] + \mu p \hat{\pi} u(c_E).$$

with $\hat{\pi}$ is the probability that bank can satisfy the fraction μ of depositors,

$$\hat{\pi} = \frac{1 - I(1 - L)}{c_E}. \quad (4)$$

Banks will have no incentive to choose risky projects, they compete for depositors who are risk averse.

Introducing deposit insurance in this model

Deposit insurance promises D to depositors in bankrupt banks.

Then bank runs are prevented if D is large enough, but:

Bankruptcy may occur also if the bank has a risky project which fails.

The insurance scheme must be financed, assume that this is done by taxing depositors.

The tax T collected should satisfy

$$TR = (1 - \pi)\mu D.$$

If there no or few banks fail, surplus B will be distributed among depositors in surviving banks.

A deviating bank

Consider a case where all banks have chosen the safe project with $q = 1$.

If a bank chooses $q < 1$, then the deposit contract should be suitably revised.

Assume that the bank proposes a contract with a markup $1/q$ on the repayment at $t = 2$.

The expected utility of a patient depositor is

$$qu \left(\frac{1}{q} \left[c_L - \frac{TR}{1 - \pi} \right] + \frac{B}{1 - \pi} \right) + (1 - q)u(D).$$

Since we consider a deviation from $q = 1$, bankruptcy will occur only due to failed projects, so probability probability $1 - q$.

Also, since only one bank deviates, we have that $B = TR$.

Deviation may be attractive

The partial derivative of expected utility wrt. q is

$$\left. \frac{\partial U}{\partial q} \right|_{q=1} = -u'(c_L) [c_L - \mu D] - u(D) + u(c_L),$$

which is < 0 when $\mu < 1$ and D is close to c_L .

Thus $q = 1$ is not an equilibrium choice when there is deposit insurance.

Alternative: **Liquidity provision**

Banks can borrow specially issued money with their assets as collateral.

In next period, banks can change back to their original assets, if not able to pay back, it defaults.