

# Economics of Banking

## Lecture 2

February 2026

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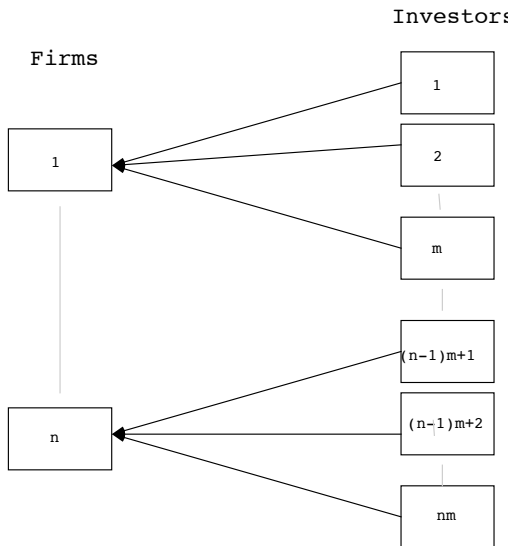
# Delegated monitoring

There are  $m$  investors each with 1 unit  
Each of them invests in  $n$  firms (spreading risk).  
Outcome is  $\tilde{y}$  (identically and independently distributed among firms).  
Assume that  $\bar{y} = E\tilde{y}$  is large enough,

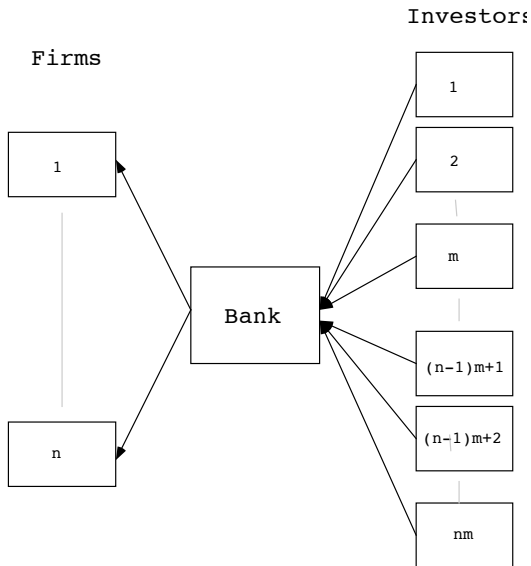
$$\bar{y} - K > 1 + r$$

(on average investment in firms is better than investment in bonds).

# Investors and firms



# With centralized monitoring



# What about incentives?

Will the put up the necessary monitoring effort in monitoring the investments?

Organize the monitor as an independent **bank** taking deposits from investors:

Deposit rate  $r_D$

The bank collects the outcomes and repays depositors with interest

But the bank may go bankrupt, namely if

$$\sum_{j=1}^n \tilde{y}_j - nK < (1 + r_D)n$$

# What is the cost of having a bank?

Average bankruptcy cost with  $n$  firms is

$$C_n = n\gamma P \left[ \sum_{j=1}^n \tilde{y}_j - nK < (1 + r_D)n \right],$$

What happens when  $n$  becomes large?

Step 1: The deposit rate  $r_D$ :

Using the bank must be as good for investors as investing in bonds:

$$E \left[ \min \left\{ \sum_{j=1}^n \frac{\tilde{y}_j}{n} - K, 1 + r_D \right\} \right] = 1 + r.$$

When  $n \rightarrow \infty$ , we have  $\sum_{j=1}^n \frac{\tilde{y}_j}{n} \rightarrow \bar{y}$  by law of large numbers.

It follows that  $1 + r_D \rightarrow 1 + r$  so that  $r_D \rightarrow r$ .

# Bank is cost saving

Step 2: Return to the bankruptcy cost which on average is

$$\frac{C_n}{n} = \gamma \mathbb{P} \left[ \frac{\sum_{j=1}^n \tilde{y}_j}{n} - K < 1 + r_D \right]$$

when  $n \rightarrow \infty$ , we use that  $\sum_{j=1}^n \frac{\tilde{y}_j}{n} \rightarrow \bar{y}$  and  $r_D \rightarrow r$ , so that

$$\frac{C_n}{n} \rightarrow 0$$

In particular

$$K + \frac{C_n}{n} < mK$$

for large enough  $n$  if  $m > 1$ .



# The moral hazard model

Two investment projects:

	$I_G$	$I_B$
Payoff if success	$G$	$B$
Prob. of success	$\pi_G$	$\pi_B$

Assume:

$B > G$  but  $\pi_G > \pi_B$  and

$$\pi_B B < 1 < \pi_G G.$$

# Incentive problem

Money market has repayment rate  $R$ .

Investor will choose  $I_G$  if

$$\pi_G(G - R) \geq \pi_B(B - R)$$

or

$$R \leq R^* = \frac{\pi_G G - \pi_B B}{\pi_G - \pi_B}.$$

# Money market may not work

Savers will demand that lending money is at least as good as storing it:

$$\pi_G R \geq 1$$

Since  $R \leq R^*$  when the market works, we have

$$\pi_G R^* \geq 1 \quad \left( \text{or } \pi_G \geq \frac{1}{R^*} \right)$$

or

$$\pi_G G - \pi_B B \geq 1 - \frac{\pi_B}{\pi_G}.$$

(moral hazard not too important)

# Monitoring saves the market

Assume that a **bank** can monitor that  $I_G$  is chosen (at a cost  $C_m$ ).  
Funding condition is then

$$\pi_G R \geq 1 + C_m.$$

Then (assuming zero profits)

$$R = \frac{1 + C_m}{\pi_G}.$$

Since  $R \leq G$ , we get

$$\pi_G \geq \frac{1 + C_m}{G}.$$

Investment can be carried through using the bank even though we may have that  $\pi_G < 1/R^*$ .

# A model of borrower behavior

Assume that a number of potential borrowers are all endowed with an investment project:

Outcome  $\tilde{y}(\theta)$  is normal with mean  $\theta$  and variance  $\sigma^2$ .

Variance  $\sigma^2$  is the same for all,  $\theta$  is individual information, not observable to others.

Investor-borrowers are risk-averse and assess their own project in such a way that their expected utility is

$$Eu(W + \tilde{y}(\theta)) = u\left(W + \theta - \frac{1}{2}\rho\sigma^2\right).$$

# Some technicalities

Where did this expression come from?

If we assume that the utility function of the borrower-investor has the form

$$u(y) = -e^{-\rho y},$$

and the variable  $w$  is normally distributed with mean  $\theta$  and variance  $\sigma^2$ , then one gets

$$\begin{aligned} E[-e^{-\rho y}] &= \int_{-\infty}^{+\infty} -e^{-\rho y} \left( \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(y-\theta)^2}{2\sigma^2}} \right) dy, \\ &= -e^{-\rho(\theta - \frac{1}{2}\rho\sigma^2)} \end{aligned}$$

The quantity  $\theta - \frac{1}{2}\rho\sigma^2$  is the *certainty equivalent* of the risky project  $\tilde{y}(\theta)$ .

# Selling projects

The market cannot observe project quality  $\theta$ , so all have a common price  $P$ .

Investor will sell only if

$$P \geq \theta - \frac{1}{2}\rho\sigma^2.$$

This is the *adverse selection*: good projects are not offered in the market, the price is too low.

Given that only bad projects are in the market, this must be reflected in the equilibrium price:

$$P = E[\theta \mid \theta \leq \theta^*],$$

where  $\theta^*$  is the best project in the market.

# Two types

Assume only two types  $\theta_1 < \theta_2$  with probability  $\pi_1$  and  $\pi_2 = 1 - \pi_1$ .

**Case 1:** If both can be sold, then  $P = \pi_1\theta_1 + (1 - \pi_1)\theta_2$  and

$$\pi_1\theta_1 + (1 - \pi_1)\theta_2 - \frac{1}{2}\rho\sigma^2 \leq \theta_2,$$

so that

$$\pi_1(\theta_2 - \theta_1) \leq \frac{1}{2}\rho\sigma^2.$$

This shows that adverse selection must be small.

**Case 2:** If adverse selection is large, then only bad projects are in the market and  $P = \theta_1$ .

Investors with good projects must develop them alone even though risk averse.



# Keeping a share

Sell only *part* of the project, keeping  $\alpha$ .

The signal of quality is the participation of the project owner. This signal is trustworthy when

$$u(W + \theta_1) \geq u(W + (1 - \alpha)\theta_2 + \alpha\theta_1 - \frac{1}{2}\rho\alpha^2\sigma^2)$$

or equivalently if

$$\theta_1 \geq (1 - \alpha)\theta_2 + \alpha\theta_1 - \frac{1}{2}\rho\alpha^2\sigma^2$$

or

$$\frac{\alpha^2}{1 - \alpha} \geq \frac{2(\theta_2 - \theta_1)}{\rho\sigma^2}.$$

Let  $\hat{\alpha}$  be the smallest share satisfying this inequality (with  $=$ ).

# Loss to seller

The financing cost to the project owner (compared with selling at full value  $\theta_2$ ), is the risk premium

$$C_f = \frac{1}{2}\rho\hat{\alpha}^2\sigma^2$$

This loss depends on  $\sigma^2$ . Indeed, we have

$$C_f = \frac{1}{2}\rho\hat{\alpha}^2\sigma^2 = (\theta_2 - \theta_1)(1 - \hat{\alpha})$$

and  $\hat{\alpha}$  is a decreasing function of  $\sigma^2$ .

# Coalitions of borrowers

Let  $n$  owners of good projects go together and create an investment pool.

Pooled project has outcome  $\sum_{j=1}^n \tilde{y}_j(\theta_2)$ ,

Variance is  $n\sigma^2$

Per unit invested the outcome is  $\frac{1}{n} \sum_{j=1}^n \tilde{y}_j(\theta_2)$ , and variance is

$$\left(\frac{1}{n}\right)^2 (n\sigma^2) = \frac{\sigma^2}{n}.$$

Cost to each investor is reduced.